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The Institute of Mathematical Sciences  
The Chinese University of Hong Kong

數學科學研究所  
香港中文大學

Phone: (852) 3943 8038 • Email: [ims@ims.cuhk.edu.hk](mailto:ims@ims.cuhk.edu.hk)  
Unit 601, 6/F., Academic Building No. 1, The Chinese University of Hong Kong, Shatin, N.T., Hong Kong

# *Joint Harvard-CUHK-YMSC Differential Geometry Seminar*

## **Counting invariant curves on a Calabi-Yau threefold with an involution**

**Abstract:** Gopakumar-Vafa invariants are integers  $n_{\beta}(g)$  which give a virtual count of genus  $g$  curves in the class  $\beta$  on a Calabi-Yau threefold. In this talk, I will give a general overview of two of the sheaf-theoretic approaches to defining these invariants: via stable pairs a la Pandharipande-Thomas (PT) and via perverse sheaves a la Maulik-Toda (MT). I will then outline a parallel theory of Gopakumar-Vafa invariants for a Calabi-Yau threefold  $X$  with an involution. They are integers  $n_{\beta}(g,h)$  which give a virtual count of curves of genus  $g$  in the class  $\beta$  which are invariant under the involution and whose quotient by the involution has genus  $h$ . I will give two definitions of  $n_{\beta}(g,h)$  which are conjectured to be equivalent, one in terms of a version of PT theory, and one in terms of a version of MT theory. These invariants can be computed and the conjecture proved in the case where  $X=S \times C$  where  $S$  is an Abelian or  $K3$  surface with a symplectic involution. In these cases, the invariants are given by formulas expressed with Jacobi modular forms. In the case where  $S$  is an Abelian surface, the specialization of  $n_{\beta}(g,h)$  to  $h=0$  recovers the count of hyperelliptic curves on Abelian surfaces first computed by B-Oberdieck-Pandharipande-Yin. This is joint work with Stephen Pietromonaco.

By

**Professor Jim Bryan**

Department of Mathematics  
University of British Columbia

**Date:** November 3, 2021 (Wednesday)  
**Time:** 9:30am – 10:30am (Hong Kong Time)  
**Zoom Link:** <https://cuhk.zoom.us/j/97402322256>  
(Meeting ID: 974 0232 2256; Passcode: 20211103)

*All are Welcome*